Adsorption of Nitrogen Monoxide and Carbon Monoxide on Copper-Exchanged ZSM-5: A Cluster and Embedded Cluster Study

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We present a systematic study on the adsorption of NO and CO in Cu–ZSM-5, using an ab initio embedded cluster methodology at the B3LYP level of theory. We found that the effects of the cluster size and Madelung potential are small for adsorption energies of CO and NO. For adsorption of CO, the calculated binding energy of 32 kcal/mol is in good agreement with experimental data from 29 to 32 kcal/mol. On the contrary, for adsorption of NO the calculated binding energy of 22 kcal/mol is much smaller than the experimental estimate, though it is consistent with recent experimental observation that NO binding energy should be smaller than that of CO. Madelung potential, however, is important for obtaining the correct blue shift of an adsorbed NO.

Introduction

Cu–ZSM-5 has been the subject of many recent theoretical and experimental studies since it was discovered to thermally and photoactivated catalyze the reduction of NO_x species.^{1–7} The adsorption of NO molecules on the active site to form nitrosyl complexes is considered the important step. Much progress in understanding the nature of the active site of the Cu–ZSM-5 zeolite has been made. However, a detailed molecular-level understanding of the mechanism of catalytic reduction of NO_x species is far from complete.

XANES, EXAFS, and photoluminescence showed that Cu(I) species are the active site for the decomposition of NO^{8-12} and almost all of Cu(II) ions in Cu-ZSM-5 can be autoreduced to Cu(I) ions during an evacuation process.⁹ CO has been frequently used as a probe molecule to obtain information about the active sites of Cu-ZSM-5 due to its high IR absorbance intensity and the stability of the Cu-ZSM-5/CO complexes.^{10,13-15} CO is known to be adsorbed on Cu-ZSM-5, even under mild conditions such as at low pressure and room temperature.¹⁶⁻²³ The frequency shift of CO in the adsorption complex has been used to depict the characteristic of the active site and its bonding nature. At least two types of Cu(I) species had been identified from previous IR experiments.^{16,17,24} The first Cu(I) species bonds symmetrically to two framework oxygen atoms, and the other bonds asymmetrically to three framework oxygen atoms. Those results agree with XAFS, IR, and UV-vis spectroscopy studies, which showed that the average coordination number of Cu(I) is 2.5 ± 0.3 .^{8–11,25} Experimental observations suggested that the first Cu(I) type is an active site for the NO_x adsorption, but both types are required for the NO_x decomposition process.

Numerous theoretical models have also been performed to provide information on the nature of the active site of Cu–ZSM-5. Several models of the active site have been proposed from the simplest model, in which a Cu cation is in fixed-

coordination with water ligands $(Cu^+[H_2O]_n)$,²⁶⁻²⁸ to more realistic ones which consist of up to six tetrahedral sites.^{18,29-35} As discussed below, these models have some mix success. Furthermore, although its coordination information has been established, the location of Cu⁺ in the zeolite framework is not known for certain. Previous HF and lattice energy minimizing calculations showed that T12 is the most stable site for Al substitution and is believed to be the type I active center.^{36,37} Such a site is reasonable from the structural point of view, since the bridging oxygens adjacent to the T12 site protrude into the intersection of main and sinusoidal channels; thus, this site provides sufficient space for small adsorbates binding to the exchanged copper ion.³⁸ For this reason, most previous theoretical works have chosen T12 as the active site's center. However, using a more accurate combined quantum/potential methodology, Sauer and co workers showed that T12 is not the most stable site for Al,³⁹ though it is among the more stable sites and there are only negligible differences in the relative energies of these sites. This issue certainly requires further study.

Understanding the adsorption of CO and NO on Cu-ZSM-5 zeolite would be the first step in studying the catalytic activity of this zeolite. Experimentally, the 2156–2157 cm⁻¹ band was attributed to the stretching frequency of adsorbed CO on the Cu(I) site.^{9,15,17,24,40} Kuroda deconvoluted this peak into two dominant peaks at 2159 and 2151 cm⁻¹, which were assigned to the stretching frequencies of CO adsorbed at Cu(I) species binding to two and three oxygen atoms, respectively. When Cu-ZSM-5 is exposed to NO gas, there are three bands appearing via IR at 2295, 1630, and 1812 cm⁻¹. The first two bands occur due to spontaneous decomposition of NO, and the last band was attributed to NO adsorbing on the Cu⁺ site.^{8,9,16,41,42} The experimental binding energies of CO and NO largely depend on many factors, e.g., the Si/Al ratio, the Cu exchanged rate, temperature, and pressure. The relative binding energy between CO and NO is still questionable. However, recent IR and adsorption experiments suggested that CO molecules bind to Cu-ZSM-5 zeolite stronger than NO molecules.24,43 Adsorption of CO and NO have also been the subject of numerous

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theoretical studies.^{18,27–30,34,35,44–50} The calculated results for adsorption energy, frequency shift, geometry, and the coordination number are still scattered due to differences in the topological structure of the model, cluster size, constraints, basis sets, and the levels of theory employed. Almost all of the previous theoretical models, except the Cu–water cluster, were not able to predict the experimental blue shift of adsorbed CO. Although the simplest Cu⁺[H₂O]_n model was able to illustrate several important characteristics of the active site, including the frequency shift of adsorbed CO, the predicted NO and CO binding energies are far below the experimental heat of adsorption values.⁵¹

One of the most important characteristics of zeolite is its complicated framework comprising of channels and pores. The simplest approximation is to only consider the active site locally and ignore the environment effects of the zeolite framework, as in the cluster model. However, there is sufficient evidence that such environment effects are significant.^{5,15,52,53} For instance, the framework of ZSM-5 significantly enhances the catalytic property of Cu-ZSM-5 over other Cu-exchanged zeolites. So we cannot refute the important role of the zeolite framework in this catalytic process. From a computational point of view, to account for the effects of the zeolite framework in the study of adsorption or reactions in zeolites has been a great challenge. The large unit cells of most zeolites, such as 288 atoms for the ZSM-5, prevent the use of an accurate periodic electronic-structure method, though some progress has been made in this direction, but at a great computational cost.^{54–61} It should be noted that periodic calculations correspond to high loading (coverage) cases.

A practical approach to account for the crystal effects of the zeolite is to embed the quantum mechanical cluster model of the active site in a classical potential field due to the extended zeolite framework. There are two embedding approaches. One is referred to as the electronic embedding method, which includes the electrostatic interactions of the infinite lattice of zeolite in the Fock matrix of a quantum mechanic cluster.⁶²⁻⁶⁶ The other is referred to as the mechanical embedding method, which represents with an analytical force field the potential from the crystal environment and the active site is treated as a quantum mechanical cluster.^{45,39,67,68} Although there are some differences in these two approaches, both have been successfully applied to studying adsorptions and reactions in zeolites. It is interesting to note that to date there has not been a systematic theoretical study focusing on the dependence of NO and CO adsorption properties on models of the active site, i.e., cluster size, Madelung potential, levels of theory.

From a theoretical point of view, to gain a qualitative understanding on the adsorption of small molecules on metalexchanged zeolite, one first needs to have some knowledge on the model dependence of adsorption properties of interest. In this study, our main objectives are (1) to provide a better understanding of the cluster and embedded cluster computational methodology in the study of adsorption/reaction in metalexchanged zeolites and (2) to predict adsorption properties for adsorption of NO and CO on Cu-ZSM-5 zeolite. The focus of our first objective is on the cluster size dependence and the effects of the Madelung potential on the NO/CO adsorption properties. This is accomplished by carrying out both cluster and embedded cluster calculations for different quantum clusters representing the active center. The focus of our second objective is on the adsorption structures, energies, and frequency shifts of the NO/CO adsorbed complexes. The results of this study are important for establishing a cost-effective methodology for

future studies on the mechanisms of both thermal and photoactivated catalytic reductions of NO_x by Cu–ZSM-5 and other metal-exchanged -ZSM-5 zeolites.

Methodology

The ZSM-5 structure was taken from the silicious ZSM-5 crystal (Figure 1a).⁶⁹ To represent the Lewis basic active site, the silicon atom of the T12 site was substituted by an aluminum atom. Note that we selected the T12 site for this study for the reason discussed above. An Cu(I) ion was added to counterbalance the negative charge of $[AIO_4]^-$. The exchanged monovalent copper ion was chosen to bind to two framework oxygen atoms (corresponding to the I2 site in ref 39), protruding in to the channel intersection as an initial guess structure.

Four clusters ranging from 3T to 10T, where T is Si- or Altetrahedral (SiO₄ or AlO₄⁻), were cut from the ZSM-5 lattice. The largest cluster, $[AlSi_9O_{16}H_{20}]^-Cu^+$, is a complete 10membered-ring cluster of the main channel of ZSM-5 (Figure 1b). This model represents the zeolite's pore structure, enclosing an active site and adsorbates. The other clusters are 7T, 5T, and 3T that have molecular structures of $[AlSi_6O_{12}H_{16}]^-Cu^+$, $[AlSi_4O_{10}H_{12}]^-Cu^+$, and $[AlSi_2O_8H_8]^-Cu^+$, respectively (see Figures 1c-e). Due to the partial covalent nature of zeolite, the boundary Si atoms of each cluster were saturated by capped hydrogen atoms located along the broken Si-O bonds in ZSM-5 lattice with an Si-H bond distance of 1.47 Å. The boundary SiH₃ groups were held fixed in all geometry optimizations.

To incorporate the environmental effects of the remaining zeolite framework, the QM clusters are embedded in a potential field of point charges. The SCREEP method was used to construct these point charges. The detailed description of the SCREEP method was previously discussed elsewhere.⁶⁴ To account for the electrostatic potential from the capped hydrogen atoms and to minimize their interactions with the external point charges, we removed the first shell of external charges closest to the QM cluster and adjusted the charge's values of the next shell to reproduce the correct classical Madelung potential calculated from the Ewald-sum method in the active site region.

Nonlocal hybrid density functional theory, particularly the B3LYP functional, was used in this study due to its consistency and reliability in zeolite systems.^{31,34,45,66,70} For practical purpose, we employed a larger basis set for the active site region, [SiOAlOSi]⁻Cu⁺, namely, the 6-31G(d) basis set for Si, Al, O, and the adsorbate; the HayWadt-VDZ_{*n*+1} ECP basis set for Cu(I) ion; and the smaller 3-21G basis set for the remaining spectator region.

Preliminary calculations for the smaller embedded model confirmed the experimental observation that adsorptions of CO and NO do not have large effects on the structure of the zeolite framework.^{51,66} Thus, to reduce the computational demand the active site and the surrounding sites, except those of the SiH₃ boundary groups, were allowed to fully relax in both cluster and embedded cluster calculations and then were held fixed in subsequent NO/CO adsorption calculations. All calculations were done using the Gaussian98 program.⁷¹

Results and Discussion

In this study, we have examined both the physical properties of CO and NO adsorptions on Cu–ZSM-5 zeolite and the factors that can affects the accuracy of the embedded cluster model, particularly the size of the quantum cluster and the Madelung potential. Thus it is natural to separate the discussion of the results into two parts, namely, model dependence and chemistry of CO and NO adsorption on Cu–ZSM-5 zeolite.



Figure 1. Cu-ZSM-5 Cluster models: (a) ZSM-5 lattice, (b) 10T cluster, (c) 7T cluster, (d) 5T cluster, and (e) 3T cluster of Cu-ZSM-5.

Our calculated results are summarized in Tables 1–3. Optimized geometrical parameters, Mulliken charges, and Cu ion binding energy of Cu–ZSM-5 calculated from both the cluster and embedded cluster methods using four different QM clusters are tabulated in Table 1. Similar results for CO and NO adsorption on Cu–ZSM-5 are listed in Tables 2 and 3, respectively.

Model Dependence. In the embedded cluster methodology, there are two main factors that can affect the accuracy of the results, namely, the size of the QM cluster and the representation of the embedded potential. It is difficult to separate the effects of these two factors. In this study, the embedding potential consists of only the long-range electrostatic contribution from the zeolite framework. As the size of the QM cluster increases,

it includes the short-range electrostatic, repulsion-dispersion, and polarization contributions from the local region of the active site in its full quantum mechanical treatment. Thus, the most accurate results from this study are from the embedded 10T cluster calculations and are used as a reference point for comparison in the discussion of model dependence.

Cu–ZSM-5 Active Site. We found that the local structure of the active site, i.e., the Cu⁺ ion binding site, is not very sensitive to the size of the QM cluster and the inclusion of the Madelung potential. As the size of the QM cluster increases from 3T to 10T, the Cu–O bond distances increase by at most 0.01 Å and the Al–O (to O1 or O2) bond distances decrease by at most 0.05 Å. The Cu–Al distance appears to converge at

TABLE 1: Structural Parameters (Å), Mulliken Charges (au), and Binding Energy (kcal/mol) of Cu-ZSM-5 Clusters

	3T			5T			7T			10T		
MFI	bare	emb^a	emb^b	bare	emb ^a	emb ^b	bare	emb ^a	emb^b	bare	emb ^a	emb^b
Cu–O1 ^c	1.980		2.003	1.990		2.006	1.994		2.012	1.998		2.013
$Cu-O2^{c}$	1.993		2.005	2.010		2.016	2.011		2.023	2.012		2.032
Cu-Al	2.743		2.767	2.725		2.748	2.732		2.758	2.732		2.764
Al-O1	1.812		1.819	1.752		1.760	1.752		1.755	1.751		1.753
Al-O2	1.780		1.785	1.748		1.757	1.747		1.748	1.748		1.745
q(Cu)	0.52	0.61	0.61	0.52	0.57	0.58	0.49	0.55	0.55	0.48	0.55	0.55
q(O)	-0.60	-0.60	-0.59	-0.60	-0.60	-0.60	-0.60	-0.60	-0.59	-0.60	-0.60	-0.60
$E_{\text{bind}}(\text{Cu})^d$	180.13		233.76	184.02		195.62	185.76		180.05	187.30		163.90

^a Unoptimized embedded cluster. ^b Optimized embedded cluster. ^c Framework oxygens. ^d Includes BSSE correction.

TABLE 2: Structural Parameters (Å and deg), Mulliken Charges (au), and Binding Energy (kcal/mol) of CO Adsorption on Cu-ZSM-5 Clusters

	Cu(I)	3Т			5T C-down		7T C-down		10T C-down	
	C-down	O-down C-down								
parameters ^a	cluster	emb	cluster	emb	cluster	emb	cluster	emb	cluster	emb
CO^b	1.126	1.139	1.137	1.136	1.138	1.134	1.138	1.135	1.137	1.136
CuC(O)	1.893	2.002^{e}	1.818	1.827	1.815	1.829	1.817	1.829	1.825	1.832
∠Cu CO	179.9	175.9 ^f	179.8	178.8	180.0	178.6	178.2	174.7	178.6	177.8
q(CO)	0.26	0.13	0.22	0.25	0.23	0.25	0.23	0.25	0.23	0.24
q(Cu)	0.74	0.54	0.36	0.43	0.33	0.37	0.30	0.36	0.29	0.37
$q(O_z)^c$		-0.60	-0.60	-0.60	-0.60	-0.60	-0.60	-0.60	-0.60	-0.60
$\overline{E}_{ ext{bind}}^d$	57.50	6.18	32.58	32.21	32.53	32.83	32.98	33.13	31.69	32.30

^{*a*} Only the adsorbate is optimized. ^{*b*} Optimized gas-phase CO bond length is 1.138 Å. ^{*c*} Average of charges on two bridging oxygen atoms. ^{*d*} Include BSSE and ZPE corrections. ^{*e*} Cu=O(C) distance. ^{*f*} ∠Cu=OC.

TABLE 3: Structural Parameters (Å and deg), Mulliken Charges (au), and Binding Energy (kcal/mol) of NO Adsorption on Cu-ZSM-5 Clusters

	Cu(I)	3T			5T		7T		10T	
	N-down	O-down	O-down N-down		N-down		N-down		N-down	
parameters ^a	cluster	emb	cluster	emb	cluster	emb	cluster	emb	cluster	emb
NO^b	1.147	1.174	1.168	1.166	1.169	1.164	1.168	1.165	1.167	1.165
Cu•••N(O)	1.871	1.952^{e}	1.815	1.822	1.814	1.826	1.815	1.823	1.821	1.824
∠Cu••NO	179.9	138.1^{f}	145.4	145.4	144.8	144.8	145.3	147.6	148.0	148.3
q(NO)	0.12	0.10	0.08	0.11	0.09	0.13	0.09	0.13	0.10	0.12
q(Cu)	0.88	0.54	0.45	0.52	0.43	0.45	0.40	0.44	0.38	0.46
$q(O_z)^c$		-0.59	-0.59	-0.59	-0.59	-0.59	-0.59	-0.59	-0.59	-0.59
${\hat E}_{{ m bind}}{}^d$	42.94	7.32	23.38	22.84	23.66	22.80	23.92	23.47	22.61	21.78

^{*a*} Only the adsorbate is optimized. ^{*b*} Optimized gas-phase NO bond length is 1.159 Å. ^{*c*} Average of charges on two bridging oxygen atoms. ^{*d*} Include BSSE and ZPE corrections. ^{*e*} Cu-O(N) distance. ^{*f*} \angle Cu-ON.

7T. Examining the convergence of the structural parameters, we found that the 3T cluster results deviate noticeable from others, thus indicating such a cluster is too small. Inclusion of the Madelung potential increases all Cu-O, Al-O, and Cu-Al bond distances. The largest variation of about 0.03 Å is in the Cu-Al bond distance. The increase in the Cu-Al bond distance would hinder the delocalization of Cu⁺ charge by the zeolite framework. This observation is further supported by the larger Cu Mulliken charge (by 0.1 au) when the Madelung potential is included (see Figure 2). Note that increasing the cluster size in bare cluster calculations does not have such an effect. Thus, the Cu⁺ charge localization is due mainly to the Madelung potential. The Cu⁺ binding energy shows the largest dependence on both the QM cluster size and the Madelung potential. From the bare cluster calculations, the Cu⁺ binding energy increases from 180.1 to 187.3 kcal/mol when the size of the QM cluster increases from 3T to 10T. The embedded calculations show the reverse trend, i.e., the binding energy decreases from 233.8 to 163.9 kcal/mol from the 3T to the 10T case. This indicates that inclusion of only the long-range Madelung potential may overestimate the Cu⁺ binding energy. The local short-range repulsion dispersion and polarization of



Figure 2. The cluster size and the Madelung potential dependences of the Cu Mulliken charge: cluster (\Box), embedded cluster (\blacksquare), CO/cluster (\bigcirc), CO/embedded cluster (\blacklozenge), NO/cluster (\diamondsuit), and NO/embedded cluster (\blacklozenge).

the zeolite framework also have a noticeable contribution in lowering the ion binding energy.

CO and NO Adsorption. Both CO and NO may bind to a Cu ion of Cu-ZSM-5 via either the C- (or N-) down or the O-down structures. The results are shown in Tables 2 and 3. We have used both bare and embedded 3T cluster models to investigate both modes of adsorption for CO and NO on Cu-ZSM-5. For both systems, the Cu-O binding distances (Cu to oxygen of CO or NO) in the O-down adsorption complexes are more than 0.13 Å longer than the corresponding C-down or N-down case. Consequently, the O-down adsorption complexes have much weaker binding energies, particularly 6.2 versus 33.2 kcal/mol for the CO/Cu-ZSM-5 complex and 7.3 versus 22.8 kcal/mol for the NO/Cu-ZSM-5 complex. For this reason, we do not expect that the O-down adsorption mode would play an important role in the chemistry of reduction of NO_x by Cu-ZSM-5 zeolite, and thus, we only concentrate our further efforts to study the C-down and N-down adsorption modes.

It is interesting to note that the structures and binding energies for adsorption of both CO and NO on Cu-ZSM-5 zeolite do not depend strongly on either the cluster size or the Madelung potential. In fact, variations in the CO and NO bond distances in the adsorption complexes are less than 0.005 Å for both bare and embedded cluster methods. Inclusion of the Madelung potential is seen to lengthen the adsorption distance (Cu-N or Cu-C bond distance) by at most 0.015 Å. Similar to the Cu-ZSM-5 zeolite, in the adsorption complexes, the Madelung potential localizes the Cu⁺ ion charge but to a lesser degree. Both the effects of the QM cluster size and the Madelung potential give rise to the variations in the CO binding energy from 31.7 to 33.2 kcal/mol and in the NO binding energy from 21.8 to 23.9 kcal/mol. It is interesting to point out the general perception that the Madelung potential tends to increase the binding energy of the adsorbate. It is not so. Our results show that the Madelung potential increases the CO binding energy by about 1 kcal/mol but decreases the NO binding energy also by about 1 kcal/mol. Although the effect of the Madelung potential is not large here, it is sufficient to illustrate the point.

In summary, with the exception of the Cu^+ ion binding energy, the structures of the Cu-ZSM-5 and its CO and NO adsorption complexes and their corresponding binding energies exhibit a rather weak dependence on the size of the quantum cluster and the inclusion of the Madelung potential. The Madelung potential, however, was found to stabilize the Cu^+ ion charge and thus reduces the charge delocalization by the zeolite framework. This would have an important implication in studying the photocatalytic activity of metal-exchanged zeolites where the charge-transfer process is thought to be an important step in the catalytic cycle. From the variations in the structures, binding energies, and Mulliken charges, we found that the embedded 5T cluster model provides a balance between computational efficiency and accuracy.

Chemistry. In this subsection, we discuss the chemistry of CO and NO adsorption on Cu-ZSM-5 and comparisons of our results with those from previous experimental and other theoretical studies. For this, we use the results from our most accurate embedded 10T cluster calculation.

Cu–ZSM-5. Previous experimental and theoretical studies have suggested that Cu⁺ ions are located at intersections between sinusoidal and main channels, exposed to diffused species. The majority of Cu⁺ ions in ZSM-5 are expected to coordinate to two bridging oxygen atoms of the active site.^{18,29,30,33,45,50,72} All structural parameters of our model, i.e., bond distances and the coordination number of the copper ion, are comparable to experimental results. Particularly, the calculated Cu–O bond distances of 2.013–2.032 Å (see Table 1) are in excellent agreement with the experimental data of 2.00 ± 0.02 Å, determined by Lamberti et al.⁸ In comparison with previous theoretical studies, our calculated Cu–O bond distances are slightly larger. In particular, Chakraborty et al.,³³ using the 5T cluster, found the two Cu–O bond lengths of 1.95 and 1.86 Å. The DFT/LSD calculations of Hass and Schneider on the 5T cluster yielded Cu–O distances of 1.919 and 1.924 Å.³⁰ Increasing cluster size and including the Madelung potential do not have large effects, though they bring the results in better agreement with experimental values. Although there is some charge redistribution between the copper ion and zeolite framework, the charge of 0.55 on the Cu⁺ ion supports the suggestion that these Cu⁺ ions prefer to exist as isolated monomer species.⁷³

Since experimental data for the Cu⁺ binding energy is not available, we compare our results to previous theoretical data. We mentioned above that the binding energy between the Cu⁺ cation and zeolite framework shows a strong dependence on the cluster size and the Madelung potential. Comparisons with previous studies further support this conclusion and also show some dependence on the levels of theory employed. In particular, Hass and Schneider used the simple 5T model at the DFT/LSDA level of theory and obtained the binding energy of 175 kcal/ mol.²⁹ Sauer and co-workers⁴⁵ determined the Cu⁺ binding energy of 160 kcal/mol from a 3T model at the DFT/B3LYP level of theory. Sauer et al.³⁹ also predicted a value of 148.6 kcal/mol from their mechanical embedded 3T cluster model (QM-pot) at the same level of theory. Our calculated binding energy with the basis set superposition error (BSSE) correction is 164 kcal/mol. The variations in these results serve as a caution for the use of cluster and embedded cluster models in studying Lewis basic sites and adsorption of ions on zeolites.

Adsorption of CO on Cu–ZSM-5. Basically, the nature of the bonding between a Cu⁺ ion and a CO molecule can be described by the back-bonding process. The HOMO orbital of CO is the $5\sigma^*$ antibonding orbital. σ donation from this orbital to the transition metal ion would strengthen both the CO bond and the Cu-CO interaction. On the other hand, the LUMO of CO is the $6\pi^*$ orbital. π accepting to this orbital, i.e., electron flows from the transition metal to the $6\pi^*$ orbital, would strengthen the Cu-CO interaction but weaken the CO bond.

CO bond length is shortened slightly upon adsorption. Our calculated Cu–O_{framework} and Cu–C distances of 2.03 and 1.832 Å are in excellent agreement with those of 2.05 and 1.89 Å determined by Nagao et al.⁵¹ using spectroscopic techniques. As expected, the Cu–C bond is slightly affected by the Madelung potential, thus supporting the observation that the Cu–C stretching frequency is much more sensitive to the zeolite structure, i.e., the long-range potential, than the CO bonding.¹⁵ The Cu–CO angle is linear (Figure 3) corresponding to previous calculation studies.^{26,27,30} The net charge of the adsorbed CO molecule is slightly positive, revealing the electron transfer from an adsorbate to the copper ion. From the shortening of the CO bond length and the decreasing of the Cu⁺ positive charge, we can conclude that the σ donating dominates the interaction between the exchanged copper and the carbonyl ligand.

One of the most important characteristics of the CO/Cu– ZSM-5 complex that can be obtained from experiment is the IR frequency of adsorbed CO. While the interaction between the bare Cu⁺ ion and a CO molecule yields the red shift of the CO stretching frequency, IR spectra of adsorption of CO on Cu–ZSM-5 yields two peaks (from two different Cu⁺ sites as mentioned above) at 2159 and 2151 cm⁻¹, which are blueshifted from the peak at 2143 cm⁻¹ of the gas-phase CO.²⁴ This





Figure 3. Optimized structure of CO/Cu-ZSM-5 complex using the embedded 10T model.

blue shift should correspond to the stronger and shorter CO bond, as observed in this study. To confirm this the stretching frequency of an adsorbed CO was calculated using our embedded 3T model. Without any scaling, the adsorbed CO frequency was determined to be 2237.7 cm⁻¹, blue-shifted from 2208.2 cm⁻¹ of the gas-phase CO. Such a blue shift was not observed in most of the previous theoretical models, even at the same cluster size and the same level of calculation. Thus the Madelung potential is expected to be important for obtaining the correct blue shift of an adsorbed CO.

The binding energies calculated from previous theoretical models are quite scattered, ranging from 25 to 54 kcal/mol.^{27,29,30,46,74} The experimental CO binding energy was determined to be 28.7 kcal/mol by Nagao et al.⁵¹ and 31.6 kcal/mol by Szanyi and Paffett (an unpublished result cited by Brand et al.²⁷). After including the BSSE correction and zero-point energy (ZPE) correction, we obtain the CO binding energy of 32.01 kcal/mol, which agrees well with experimental values.

In this study, we found an "anticorrelation" between binding energy and bond distance. If the bonding between an ion and an adsorbate is dominated by electrostatic interaction, one can expect that the binding energy decreases upon increasing the bond distance. Our results show that while the binding energy between the bare Cu⁺ ion with CO (57.5 kcal/mol) is much larger than that (32.3 kcal/mol) of the Cu–ZSM-5/CO complex, the Cu–C bond distance is longer, 1.893 Å compared to 1.832 Å. This indicates that the interactions between the Cu⁺ site in ZSM-5 zeolite and CO are more complex than just an electrostatic one. This supports the previous suggestion that the combination of electrostatic interaction, between CO molecule and zeolitic framework, and σ donation, between CO and exchanged copper ion, induces a blue shift of adsorbed CO.⁷⁵

Adsorption of NO on Cu–ZSM-5.

The HOMO of NO molecule is the $6\pi^*$ orbital. The electron transfer from the copper's d-orbital to this orbital in the π accepting process increases the Cu⁺-NO interaction but simultaneously decreases the NO bond order, i.e., elongates the NO bond distance while the π and σ donating (from $5\sigma^*$ and $6\pi^*$ orbitals) would increase the Cu⁺-NO interaction and NO bond order, i.e., shorten the NO bond distance.



Figure 4. Optimized structure of NO/Cu-ZSM-5 complex using the embedded 10T model.

Our calculated NO bond distance in the NO/Cu-ZSM-5 complex is 1.165 Å, which is longer than the gas-phase value of 1.159 Å. Previous theoretical studies have also observed this elongation of the NO bond. This indicates that π accepting is the dominant process, which is opposite of the CO/Cu-ZSM-5 case. It is interesting to point out that for the bare Cu⁺ ion/NO complex, the NO bond distance is shortened to 1.147 Å and thus σ donating is preferred (molecular charge of adsorbed NO compared to free NO). These results show that the zeolite framework is important in determining the nature of the bonding between the exchanged Cu⁺ ion and the adsorbate. From IR studies, the NO stretching vibration at 1810 cm⁻¹ was assigned to linearly adsorbed NO, since generally NO frequencies that are larger than 1720 cm⁻¹ correspond to linear species.^{18,76,77} Our Cu-NO angle of 148° (see Figure 4) differs drastically from this suggestion and also from the CO/Cu-ZSM-5 case (see Figure 3). This appears to be a contradiction between our result and experiment. Since the interaction between the Cu⁺ ion and NO is dominated by the π accepting, one can expect that the Cu-NO configuration should be bent to have a positive overlap with Cu's d orbital (the linear configuration would yield zerooverlap). This is different from the CO/Cu-ZSM-5 system, where the σ donating is the dominant process and the linear configuration would have the largest overlap. To further understand the difference between our result and the experimental observation, we plotted a potential curve as the function of the Cu-NO angle, as shown in Figure 5. From the overlap argument above one can expect the linear configuration to be the saddle point between the two symmetrical bent structures. Figure 5 confirms our expectation, and the barrier for converting between the two stable bent structures is only 1 kcal/mol.²⁶ This suggests that experiments would observe the average of the thermal fluctuation between the two stable bent structures, i.e., the linear configuration. Thus, our results provide a deeper understanding of the adsorption structure of NO on Cu-ZSM-5.

The NO stretching frequency of the NO/Cu–ZSM-5 complex, observed experimentally at 1812 cm^{-1} , is red-shifted from 1860 cm⁻¹ of the gas-phase NO.⁴² This red shift corresponds to the lengthening of the NO bond, observed in our study and other theoretical works.^{27,29,32,46,47} The stretching frequency of an adsorbed NO was calculated using our embedded 3T model to be 1921.7 cm⁻¹, red-shifted from 1990.4 cm⁻¹ of the gas-phase NO.



Figure 5. Potential energy curve, relative to the stable NO/Cu-ZSM-5 complex as a function of Cu-NO angle.



Figure 6. Comparison between calculated and experimental binding energies, for the CO/Cu−ZSM-5 system: the present embedded results (upper solid line), bare cluster results (upper dashed line), experimental range (light shade area, from refs 27 and 51), and previous theoretical predictions (large \blacklozenge from ref 27; large **x** from ref 46; large **■** from ref 30). For the NO/Cu−ZSM-5 system: the present embedded results (lower solid line), bare cluster results (lower dashed line), experimental range (dark shade area, from ref 18) and previous theoretical predictions (small \blacklozenge from ref 27; small **x** from ref 46; small **■** from ref 30 and * from ref 79).

Our calculated binding energy of NO to the Cu-ZSM-5, including the BSSE and ZPE corrections, is about 22 kcal/mol. Note that previous calculated binding energies of NO adsorption are very scattered, ranging from 17 to 52 kcal/mol, as shown in Figure 6.18,29,30,34,44,46,47,78,79 The NO binding energy estimated by Chakraborty et al.¹⁸ from TPD results of Li and Armor is 43.9-49.5 kcal/mol and that estimated from Schay and Guczi's results is 47.6-49.5 kcal/mol. These experimental estimations are much higher than our prediction for the NO binding energy and higher than the experimental CO binding energy as well. However, recent experiments on successive adsorption of CO and NO15,16 found that CO molecules can displace NO molecules adsorbed on the active site of Cu-ZSM-5. This indicates that the binding energy of NO should be smaller than that of CO and thus supports our results. Note that our relative CO/NO binding energies (32.3/21.8 kcal/mol) are consistent with those from the previous calculations of Schneider et al. (40.9/38.5 kcal/mol)²⁶ and Brand et al. (24.7/17.0 kcal/mol).²⁷ Furthermore, the binding energy of NO to Cu-Zeolite-Y was determined to be 20 kcal/mol by IR spectroscopy,80 and a different absorption experiment also showed that NO can bind to the Cu-ZSM-5 tighter than to the Cu-Zeolite-Y.53 Due to the fact that Zeolite-Y and ZSM-5 have the same order of pore size, the binding

energies of NO to these zeolites should not be too different. Combining all of these experimental facts, the NO binding energy should be slightly larger than 20 kcal/mol and thus fully consistent with our results.

Conclusions

We presented a systematic theoretical study on the structure of the Lewis basic active site of the Cu-ZSM-5 zeolite and the adsorption properties of NO and CO on this zeolite. Both cluster and embedded cluster methodologies were employed to study the effects of the cluster size and of the Madelung potential. From a theoretical point of view, we found that the effects of the cluster size and of the Madelung potential are small in the NO and CO adsorption properties. However, these effects are noticeable in the Cu⁺ binding energy. Comparing all models considered in this study ranging from 3T to 10T, the 5T cluster gives the optimal cost per performance ratio and thus provides a more practical model for future studies on this system. For NO and CO adsorption, we found that the zeolite framework plays a significant role in the adsorption mechanism. The calculated adsorption properties, namely, adsorption structure, binding energy, and vibrational frequency of CO on Cu-ZSM-5 zeolite, agree well with available experimental results. Compared to previous studies, the Madelung potential is expected to contribute the correct blue shift of an adsorbed CO and red shift of an adsorbed NO. Particularly, the calculated CO binding energy of 32.3 kcal/mol is in excellent agreement with the available experimental data from 29 to 32 kcal/mol. For NO adsorption, we were able to explain to the difference between our predictions of the bent adsorption structure with the experimentally observed linear structure. The calculated NO binding energy of 21.8 kcal/mol is smaller than the estimated experimental values ranging from 44 to 50 kcal/mol. However, our result is consistent with recent experimental observation that the NO binding energy should be smaller than that of CO and is within the range of NO binding energy in the similarly pore sized Cu-Y zeolite. The calculated red shift in the adsorbed NO stretching frequency also agrees well with experiments.

The study further supports the use of the embedded cluster model to study adsorption in zeolites, particularly metal-exchanged zeolites, and establishes a foundation for future studies of the catalytic activity of Cu–ZSM-5 in reduction of NO_x species.

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